

Planens skärning

$$\begin{cases} x+y+3z+6=0 \\ 2x+y-2z-10=0 \end{cases} \Leftrightarrow \begin{cases} x+y+3z+6=0 \\ -y-8z-22=0 \end{cases} \Leftrightarrow$$

$$\Leftrightarrow \begin{cases} x = 5t + 16 \\ y = -8t - 22 \\ z = t \end{cases} \quad (l_1)$$

Linjen genom  $(6, 0, 1)$  och  $(-4, 4, -7)$

$$\begin{cases} x = 6 - 10t \\ y = 0 + 4t \\ z = 1 - 8t \end{cases} \quad (l_2)$$

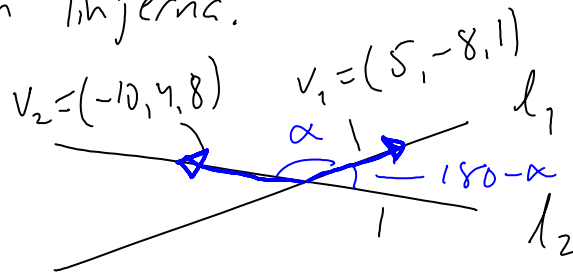
Eventuell skärning mellan linjerna.

$$\begin{cases} 5t + 16 = 6 - 10s \\ -8t - 22 = 0 + 4s \\ t = 1 - 8s \end{cases} \Leftrightarrow \begin{cases} 5 - 40s + 16 = 6 - 10s \\ -8 + 64s - 22 = 4s \\ t = 1 - 8s \end{cases}$$

$$\Leftrightarrow \begin{cases} 30s = 15 \\ 60s = 30 \\ t = 1 - 8s \end{cases} \Leftrightarrow \begin{cases} s = \frac{1}{2} \\ t = -3 \end{cases} \quad \begin{array}{l} \text{lösbart} \\ \Rightarrow \\ \text{linjernas skär.} \end{array}$$

Skärningspunkt :  $(1, 2, -3)$

Vinkel mellan linjerna.



$$\begin{aligned} \cos \alpha &= \frac{v_1 \cdot v_2}{|v_1| \cdot |v_2|} = \frac{-50 - 32 - 8}{\sqrt{90} \cdot 2 \cdot \sqrt{45}} = \frac{-45}{\sqrt{2} \cdot \sqrt{45} \cdot \sqrt{45}} \\ &= -\frac{1}{\sqrt{2}} \quad \Rightarrow \quad \alpha = 135^\circ = \frac{3\pi}{4} \end{aligned}$$

En av vektorerna pekar tydligen "åt fel

håll". Vinkeln mellan blir  $180^\circ - 135^\circ = 45^\circ = \frac{\pi}{4}$